

AMENDMENTS TO THE SPECIFICATION

Please replace paragraph [0050] with the following amended paragraph.

[0050] The content publisher generates the sharing polynomial $f(x)$ ~~over a finite field Z_N~~ where $a_0 = SK$. Although polynomial interpolation is described, other collections of functions may also be utilized. Each partial secret share S_i may then be calculated using Equation (3), which is shown as follows:

$$S_i = f(id_i) \bmod \underline{N\phi(N)}, \quad (3)$$

where N is a RSA modulus and $\phi(N)$ is a Euler totient function.

Please replace paragraph [0053] with the following amended paragraph.

[0053] At block 514, for instance, the content publisher may broadcast k public witnesses of the sharing polynomial's coefficients, which are denoted as $\{g^{a_0}, \dots, g^{a_{k-1}}\}$, where ~~$g \in Z_N$~~ $g \in Z_N^*$. After broadcast, the content publisher may destroy the polynomial.

At block 516, each license authority id_i verifies validity of the received partial secret share. Validity may be checked by determining if Equation (4), as shown below, holds for the received partial secret share S_i utilizing the sharing polynomial's coefficients which were broadcast at block 514:

$$g^{S_i} = g^{a_0} \cdot (g^{a_1})^{id_i} \cdot \dots \cdot (g^{a_{k-1}})^{id_i^{k-1}} \bmod \underline{N} \quad (4)$$

In this way, each license authority id_i , may verify the validity of the received partial secret share S_i without exposing or knowing the secret, i.e. the private key SK .

Please replace paragraph [0063] with the following amended paragraph.

[0063] At block 620, the content player, when executed by the client device, determines if k correct partial licenses have been received by validating each of the partial licenses. The partial licenses may be validated as follows. First, node p calculates

$$g^{S_i} = g^{a_0} \cdot (g^{a_1})^{id_i} \cdot \dots \cdot (g^{a_{k-1}})^{id_i^{k-1}} \pmod{N} \quad (7)$$

from the public witnesses of the sharing polynomial's coefficients, as was described in relation to block 516 of FIG. 5 and Equation (4). Equation (6) is then applied to g^{S_i} and the received partial license $prel_i$, A_1 , and A_2 to calculate c . The received partial license $prel_i$ is verified by checking if the following equations hold: $g^r \cdot (g^{S_i})^c = A_1$ and $prel_i^r \cdot (prel_i)^c = A_2$. The above steps are repeated until the node p obtains k valid partial licenses. If k valid partial licenses cannot be obtained, generation of the formal-license fails (block 622).

Please replace paragraph [0064] with the following amended paragraph.

[0064] If k valid partial licenses are obtained, then at block 624, the content player combines the partial licenses to form the formal license. For example, the node p uses the k valid partial results to calculate the formal license utilizing Equation (8):

$$\begin{aligned}
license &= \prod_i (prel_i)^{l_{id_i}(0)} = (prel)^{\sum_i S_i \cdot l_{id_i}(0)} \\
&= (prel)^{SK} = ((license)^{PK})^{SK} \bmod N,
\end{aligned} \tag{8}$$

$$\text{where } l_{id_i}(x) = \prod_{j=1, j \neq i}^k \frac{x - id_j}{id_i - id_j}.$$

Please replace paragraph [0075] with the following amended paragraph.

[0075] At periodic intervals, for example, the license authorities may update their respective shares of the private key SK through execution of the respective update module 222 of FIG. 2. At block 802, each license authority i generates a random (k, m) sharing of the secret 0 using a random update polynomial $f_{i, \text{update}}(x)$, as shown in Equation (9):

$$f_{i, \text{update}}(x) = b_{i,1}x + \dots + b_{i,k-1}x^{k-1} \bmod N \tag{9}$$